

Faculty of Science Course Syllabus Department of Mathematics and Statistics MATH 3300 Optimization Fall 2018

LSC 244

Instructor:Mr. C. DeGagneLectures:TR 8:35-9:55Office HoursMW 11:30-12:30

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Learning Centre

Chase 328

Course Description

An introduction to the concepts and applications of linear programming. Topics include the simplex method for linear programming, duality and sensitivity analysis. Some of these topics are illustrated by means of interactive computer packages.

Course Prerequisites

A passing grade in MATH 1030.03.

Course Objectives/Learning Outcomes

This course presents the theory, application, and algorithms relevant to solving linear programming problems. In this course, students will achieve the following outcomes:

Student will:

- 1) Be able to mathematically formulate an applied word problem involving revenue, costs, and constraints as a linear program.
- 2) Be able to geometrically solve a linear program in two variables.
- 3) Be able to convert a linear programing problem into standard form.
- 4) Be able to apply the simplex algorithm to solve a linear programming problem.
- 5) Be able to find alternate solutions to a linear program problem.
- 6) Be able to utilize computer software to solve a linear programming problem.
- 7) Be able to solve a linear programming problem using either the M-Method or the Two-Phase Simplex Method.
- 8) Be able to solve a linear programming with unrestricted-in-sign variables.
- 9) Be able to analyze small changes to a linear programming problem.
- 10) Be able to produce the dual of a linear program.
- 11) Be able to describe the Dual Theorem and its consequences.
- 12) Be able to use shadow prices to analyze changes to a linear programming problem's optimal solution.
- 13) Be able to use duality to analyze changes to a linear programming problem's optimal solution.



Course Materials

We will be using the textbook *Operations Research: applications and Algorithms (4th Ed.)* by W. L. Winston, Brooks/Cole, Belmont, 2004. The textbook will be useful, but is not required. The course website will be on **BrightSpace**.

Class Content Outline

The course will be structured into the following weeks.

Lecture Date	Sections	Topics				
Sept. 4	2.1 – 2.6	Matrices and Vectors, Matrices and Systems of Linear				
		Equations, The Gauss-Jordan Method for Solving Systems of				
		Linear Equations, Linear Independence and Linear				
		Dependence, The Inverse of a Matrix, Determinants				
Sept. 6	3.1	What is a linear programming problem?				
Sept. 11	3.2	The graphical solution of two-variable linear programming problems				
Sept. 13	3.3, 3.4, 3.5, 3.8	Special cases, a diet problem, a work-scheduling problem, Blending problems				
Sept. 18	4.1, 4.2	How to convert an LP to standard form continued, preview of the simplex algorithm				
Sept. 20	4.5 <i>,</i> 4.6	Simplex algorithm, using the simplex algorithm to solve minimization problems				
Sept. 25	4.7, 4.3, 4.8	Alternative optimal solutions, direction of unboundedness, and unbounded LPs				
Sept. 27	4.12	The Big M method				
Oct. 2	4.13	The two-phase simplex method				
Oct. 4	6.1, 6.2	A graphical introduction to Sensitivity Analysis, some important formulas				
Oct. 9	Assignment 3	Groups will go to the locations for assignment 3				
Oct. 11	Assignment 3	Groups will go to the locations for assignment 3				
Oct. 16	Midterm	8:00AM to 10:00AM - Chapters 3 and 4				
Oct. 18	6.2	Some Important Formulas continued				
Oct. 23	Assignment 3	Group presentations				
Oct. 25	Assignment 3	Group presentations				
Oct. 30	6.3	Sensitivity Analysis				
Nov. 1	6.5, 6.7	Finding the Dual of an LP, the dual theorem and its consequences				
Nov. 6	6.8, 6.9	Shadow prices, Duality and Sensitivity Analysis				
Nov. 8						
Nov. 13	No Class	November Break				
Nov. 15	No Class	November Break				
Nov. 20	Test	Chapter 6				
Nov. 22	9.1, 9.2	Introduction to Integer Programming, Formulating Integer Programming problems				



Nov. 27	9.3, 9.5	The Branch-and-Bound method for solving pure integer programming problems, Solving Knapsack problems by the Branch-and-Bound method
Nov. 29	Review	
Dec. 4	No Class	

Course Assessment Component

Component	Weight (% of final grade)	Date		
Assignments	25%	Due: Sept. 11, Sept 25, Oct. 9,		
		Oct 30, Nov. 22		
Test	10%	Nov. 20 in class		
Midterm	20%	Oct. 16 in class		
Final	45%	Scheduled by Registrar		

Conversion of numerical grades to Final Letter Grades follows the Dalhousie Common Grade Scale

A+	(90-100)	B+	(77-79)	C+	(65-69)	D	(50-54)
А	(85-89)	В	(73-76)	С	(60-64)	F	(<50)
A-	(80-84)	B-	(70-72)	C-	(55-59)		

Course Policies

- 1) Late assignments may be accepted with a valid reason, until solutions are posted, after which no late assignments can be accepted.
- 2) Missed assignments, with a valid reason, will be dealt with on an individual basis.
- 3) You are allowed to discuss your work with your class mates when solving the assignment problems, but you are required to do your final write-up by yourself.
- 4) Assignments will focus on feedback. Grades will be given, but the purpose of these assignments is to grow and to prepare you for the midterm and exam. Each question will be weighted out of four: 0 for not doing the question, 1 for struggling with the question (a lot of feedback), 2 for having a good idea of the methods, but still needing improvement, 3 for almost getting the question but not quite (little feedback), and 4 for the correct solution.
- 5) This course will only be cancelled in relation to weather related emergencies when the university is officially closed. If homework was due on that date it will be due on the date of the next scheduled class for this course.
- 6) There will be no makeup midterm or test. If you miss the midterm without **prior** permission, then it will count as a zero. Exceptions are made in two cases: (1) if you obtain the instructor's permission **prior** to a midterm or test, or (2) if you miss a midterm or test for a medical reason and have a doctor's note (you must notify the instructor **prior** to the midterm/test, and provide a medical note upon your return). In these cases, the weight of the missed midterm/test will be shifted to the final exam (so, for example, your final exam will be worth 65% of your final grade if you miss the midterm).
- 7) It will not be possible to write the final exam early and there will only be a make-up of the final exam in case of illness or family emergencies. So do not schedule your flight home before the final exam date.



 Office hours will be on Mondays and Wednesdays from 1 until 2 in the Learning Centre. However, help will be given on the Discussions page on Brightspace, so students are encouraged to use that.

Brightspace Discussions

There will be a thread in the Discussions page on Brightspace for each assignment, as well as a section for students to post questions they have found either in the textbook or in other sources. This is meant to be a safe and friendly environment for students seeking help to post and ask questions. However, if you are answering a post on an assignment question you may only post hints/tips to aide the other student. Do not post solutions to assignments. You may post outside links as long as they are meant to help and not the solution (some Math Overflow or Math Stack Exchange will be tolerable under the condition that the answers given on the page are hints and not solutions).

University Policies and Statements

This course is governed by the academic rules and regulations set forth in the University Calendar and by Senate

Academic Integrity

At Dalhousie University, we are guided in all of our work by the values of academic integrity: honesty, trust, fairness, responsibility and respect (The Center for Academic Integrity, Duke University, 1999). As a student, you are required to demonstrate these values in all of the work you do. The University provides policies and procedures that every member of the university community is required to follow to ensure academic integrity.

Information: https://www.dal.ca/dept/university_secretariat/academic-integrity.html

Accessibility

The Advising and Access Services Centre is Dalhousie's centre of expertise for student accessibility and accommodation. The advising team works with students who request accommodation as a result of a disability, religious obligation, or any barrier related to any other characteristic protected under Human Rights legislation (Canada and Nova Scotia).

Information: https://www.dal.ca/campus_life/academic-support/accessibility.html

Student Code of Conduct

Everyone at Dalhousie is expected to treat others with dignity and respect. The Code of Student Conduct allows Dalhousie to take disciplinary action if students don't follow this community expectation. When appropriate, violations of the code can be resolved in a reasonable and informal manner—perhaps through a restorative justice process. If an informal resolution can't be reached, or would be inappropriate, procedures exist for formal dispute resolution.

Code: <u>https://www.dal.ca/dept/university_secretariat/policies/student-life/code-of-student-conduct.html</u>



Diversity and Inclusion – Culture of Respect

Every person at Dalhousie has a right to be respected and safe. We believe inclusiveness is fundamental to education. We stand for equality. Dalhousie is strengthened in our diversity. We are a respectful and inclusive community. We are committed to being a place where everyone feels welcome and supported, which is why our Strategic Direction prioritizes fostering a culture of diversity and inclusiveness

Statement: http://www.dal.ca/cultureofrespect.html)

Recognition of Mi'kmaq Territory

Dalhousie University would like to acknowledge that the University is on Traditional Mi'kmaq Territory. The Elders in Residence program provides students with access to First Nations elders for guidance, counsel and support. Visit the office (Rm 3037, McCain Building), e-mail (<u>elders@dal.ca</u>) or leave message (902-494-6803).

Information: https://www.dal.ca/campus_life/communities/native.html

Important Dates in the Academic Year (including add/drop dates) <u>https://www.dal.ca/academics/important_dates.html</u>

University Grading Practices

<u>https://www.dal.ca/dept/university_secretariat/policies/academic/grading-practices-policy.html</u>



Student Resources and Support

Advising

General Advising https://www.dal.ca/campus_life/academic-support/advising.html

Science Program Advisors: https://www.dal.ca/faculty/science/current-students/academic-advising.html

Aboriginal Student Centre: https://www.dal.ca/campus_life/communities/native.html

Black Advising Centre: https://www.dal.ca/campus_life/communities/black-student-advising.html

International Centre: https://www.dal.ca/campus life/international-centre/current-students.html

Academic supports

Library: https://libraries.dal.ca/ Writing Centre: https://www.dal.ca/campus_life/academic-support/writing-and-study-skills.html Studying for Success: https://www.dal.ca/campus_life/academic-support/study-skills-and-tutoring.html Copyright Office: https://libraries.dal.ca/services/copyright-office.html Fair Dealing Guidelines https://libraries.dal.ca/services/copyright-office/fair-dealing.html

Other supports and services

Student Health Services: <u>https://www.dal.ca/campus_life/health-and-wellness/health-</u> services/services.html

Counselling: https://www.dal.ca/campus life/health-and-wellness/counselling.html

Student Advocacy: <u>https://www.dsu.ca/services/community-student-services/student-advocacy-service</u>

Ombudsperson: <u>https://www.dal.ca/campus_life/safety-respect/student-rights-and-responsibilities/where-to-get-help/ombudsperson.html</u>

Safety

Research Lab Safety

https://www.dal.ca/content/dam/dalhousie/pdf/dept/safety/lab_policy_manual_2007.pdf

Biosafety: https://www.dal.ca/dept/safety/programs-services/biosafety.html

Chemical Safety: https://www.dal.ca/dept/safety/programs-services/chemical-safety.html

Radiation Safety: https://www.dal.ca/dept/safety/programs-services/radiation-safety.html

Scent-Free Program: https://www.dal.ca/dept/safety/programs-services/occupational-safety/scent-free.html