

Faculty of Science Course Syllabus Department of Economics Math Workshop Fall 2023/2024

Dalhousie University is located in Mi'kma'ki, the ancestral and unceded territory of the Mi'kmaq. We are all Treaty people. We acknowledge the histories, contributions, and legacies of the African Nova Scotian people and communities who have been here for over 400 years

Instructor

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Course Description

This mathematics workshop is designed to provide economics students with essential mathematical tools to excel in their core courses, including Macroeconomics, Microeconomics, and Econometrics, as well as other elective economics courses. Throughout the workshop, students will engage in interactive sessions and practical exercises that focus on key mathematical concepts relevant to economics. The course will cover fundamental topics such as calculus, linear algebra, optimization, and probability theory, with an emphasis on their applications in economic analysis.

Course Material

Textbook: *Fundamental Methods of Mathematical Economics* by Alpha Chiang (1984) Textbook: *Mathematical Methods for Economics* by Michael W. Klein (2002) Textbook: *Mathematics for Economists* by Carl P. Simon and Lawrence Blume (1994) Textbook: *Introductory Econometrics: A Modern Approach* by Jeffrey M. Wooldridge (2019)

Students are also welcome to refer to a recommended website by Martin J. Osborne found below. This website provides a deep review of the math needed for an economics student and will be referred to during the workshop.

https://mjo.osborne.economics.utoronto.ca/index.php/tutorial/index/1/toc.

| Topics | Content | Suggested Reading |
|--|---|--|
| Basic Review | Mathematical notation; proofs; properties of functions; types of functions; graphical representation of functions | Chiang \rightarrow Ch.1-2, 6.4-6.6, 10; Klein \rightarrow Ch.1-3; Simon & Blume \rightarrow Ch.1-2, 5; Osborne \rightarrow 1.1, 1.4, and 1.7 |
| Matrix & Linear Algebra | Matrix operations; systems of linear equa- tions; determinants; inverse of a ma- trix; rank; Cramer's rule; eigen values and eigen vectors; differentiation of ma- trices/vectors | Chiang \rightarrow Ch.3-5; Klein \rightarrow Ch.4-5; Simon & Blume \rightarrow Ch.6-11; Osborne \rightarrow 1.2 and 1.3; Wooldridge \rightarrow Appendix D |
| Differential Calculus | Derivatives; differentiation; rules of dif- ferentiation; chain rule; Taylor theorem; partial derivatives; homogenous func- tions; Euler's theorem; implicit functions; comparative statics | Chiang \rightarrow Ch.6-8; Klein \rightarrow Ch.6-8; Simon & Blume \rightarrow Ch.3-4, 14; Osborne \rightarrow 1.5, 1.6, 2.1-2 |
| Concavity & Convexity | Definitions; convex sets; definiteness and semi-definiteness of a matrix; concave and convex functions; quasiconcavity and quasiconvexity | Simon & Blume \rightarrow Ch.21; Osborne \rightarrow 3.1-3.4; TBD |
| Optimization | Extreme values; first and second order conditions (uni-and multi-variate cases); necessary and sufficient conditions; Hes- sian matrix; unconstrained vs. con- strained optimization; envelope theo- rem; bordered Hessian; Lagrange tech- nique; Kuhn-Tucker method (inequality constraints); economic applications | Chiang \rightarrow Ch.9, 11, 12; Klein \rightarrow Ch. 9-11; Simon & Blume \rightarrow Ch.17-19; Osborne \rightarrow 4.1-4.3, 5.1-5.3, 6.1-6.3, 7.1-7.5 |
| Integral Calculus | Indefinite integrals; definite integrals; rules of integration; improper integrals; economic applications | Chiang \rightarrow Ch.14; Osborne \rightarrow 1.5; TBD |
| Dynamic Optimization and Dynamic program- ming | Finite vs. infinite horizon models; discrete vs. continuous settings; etc. | TBD |

Table 1: Topics Covered and Suggested Readings

Tentative Schedule

| Date | Time | Building | Room | Topics Covered |
|----------|---------------|----------|------|--|
| Sept. 5 | 16:05 - 18:05 | | | Basic Review |
| Sept. 6 | 16:05 - 18:05 | | | Matrix and Linear Algebra |
| Sept. 7 | 16:05 - 18:05 | | | Differential Calculus |
| Sept. 8 | 10:00 - 12:00 | | | Differential Calculus |
| Sept. 8 | 16:05 - 18:05 | | | Concavity and Convexity |
| Sept. 11 | 16:05 - 18:05 | | | Concavity and Convexity; Optimization |
| Sept. 12 | 16:05 - 18:05 | | | Optimization |
| Sept. 13 | 16:05 - 18:05 | | | Optimization |
| Sept. 14 | 16:05 - 18:05 | | | Optimization; Integral Calculus |
| Sept. 15 | 10:00 - 12:00 | | | Integral Calculus |
| Sept. 15 | 16:05 - 18:05 | | | Dynamic Optimization and Dynamic Programming |
| Sept. 18 | 16:05 - 18:05 | | | Dynamic Optimization and Dynamic Programming |
| Sept. 19 | 16:05 - 18:05 | | | Dynamic Optimization and Dynamic Programming |
| Sept. 20 | 16:05 - 18:05 | | | Dynamic Optimization and Dynamic Programming |

The following is a *tentative* schedule for the workshop.